Resonance penetration of intense femtosecond laser pulses through dense plasma of ultra-thin foils

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Outlook

- Transmission coefficient for penetration of intense femtosecond laser pulse through dense plasma of an ultra-thin foil has been derived, as a function of foil thickness, analytically for the first time using the one-dimensional Vlasov-Boltzmann equation and taking into account absorption of radiation.
- Foil is destroyed only after termination of ultrashort femtosecond laser pulse.
We consider only bulk free electrons inside the foil and do not consider small part of strongly heated electrons.
Maxwell-Vlasov-Boltzmann kinetic equations for the distribution function $\delta f$ is of the form

$$i\omega \delta f - v_z \frac{d}{dz} \delta f = F(z) \frac{\partial f_0}{\partial v_x} - i\omega \frac{dF(z)}{dz} \left[ v_x \frac{\partial f_0}{\partial v_z} - v_z \frac{\partial f_0}{\partial v_x} \right] - \frac{\delta f}{\tau}$$

$$\frac{d^2 F(z)}{dz^2} = -\frac{4\pi i\omega}{c^2} \int v_x \delta f dv_x dv_z$$

$\tau$ is the time between collisions of an electron with an atomic ion inside the foil plasma resulting in induced inverse bremsstrahlung;

$f_0$ is unperturbed distribution function;

$F(z)$ is the field strength amplitude inside the foil;

plasma frequency $\omega_p >>$ laser frequency $\omega$
Foil electrons are reflected elastically from both foil boundaries (as at the anomalous skin-effect)

We assume

\[ f_0 \left( v_x, v_z \right) \square \delta \left( v_z^2 - v^2 \right) \]

Integro-differential equation for the electric field strength in the absence of absorption:

\[
\frac{d^2 E(z)}{dz^2} - \frac{\omega_L^2 \Delta}{c^2} E(z) = \frac{\omega}{c^2} \frac{\omega_L^2 (1 - \Delta)}{v} \times \\
\times \left\{ \int_0^z d z' E(z') \sin \left[ \frac{\omega}{v} (z - z') \right] + \frac{\cos(\omega z / v)}{\sin(\omega d / v)} \int_0^d d z' E(z') \cos \left[ \frac{\omega}{v} (d - z') \right] \right\}.
\]

\[ \Delta = 1 - v_x^2 / v^2 \]

It has been solved analytically!
Dependence of the transmission coefficient on the dimensionless foil thickness $D = \frac{d\omega}{\nu}$ when there is no transverse electron motion ($\nu_x = 0$)

In the numerical example we consider the typical case when $E_z = 1.5$ keV, i.e. $\nu/c = 0.08$.

The photon energy of Ti:Sapphire laser is $\hbar\omega = 1.5$ eV.

one obtains the well known damping of the electric field inside the foil on the skin depth of the order of 100 - 150 Å
Resonance dependence of the transmission coefficient on the foil thickness \( D = d \omega / \nu \) when transverse electron energy is equal to its longitudinal energy.
Resonance dependence of the transmission coefficient on the foil thickness $D = d\omega/\nu$ when transverse electron energy is equal to twice of its longitudinal energy.

Figure 3
Resonance dependence of the transmission coefficient on the foil thickness $D = d\omega / \nu$ when transverse electron energy $E_x$ is equal to $6E_z$.

$\Delta d \equiv \frac{\pi \nu}{\omega}$

is the distance between the neighboring resonances.
Conclusions

• We predict a non-monotonic behavior of the transmission coefficient with several peaks as a function of the ultra-thin foil thickness. Unlike results of Ref. (G. Ferrante, and S.A. Uryupin, Phys. Lett. A 345, 205, 2005), it can be observed also at isotropic velocity distribution of bulk electrons in foil plasma. The distance between resonances is of the order of \[ \frac{\pi v}{\omega} \]
Conclusions

- This effect can be used for measurements of the width of super-thin foils.
- For example, at the electron energy of 1.5 keV in all directions and Ti:Sapphire laser we obtain that this distance is of the order of 35 nm.